


Hybridization of Description Logics and Logic Programming

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Abstract. Thales³ aims to develop a virtual assistant to support pilots during flights, with a central component being the knowledge base. This knowledge base is built using a knowledge representation(KR) and reasoning system, encompassing various knowledge types including static and dynamic. However, existing KR systems present some limitations which include expressiveness and reasoning performance. The problem of expressiveness can be addressed by integrating two distinct KR concepts: Rules and Ontologies.

Ontologies offers a framework for formalizing concepts, properties, and relationships, whereas rules express knowledge through IF-Then constructs. Integrating these approaches enriches knowledge representation and reasoning systems in many ways and helps to achieve completeness. However, this integration poses challenges, such as the difficulty of aligning their semantics and addressing issues of decidability. This thesis focuses on defining a methodology to combine rules and ontologies to overcome these challenges and build an optimized reasoner to execute the reasoning tasks of the virtual assistant ensuring good performance.

Keywords: Description Logic · Rules · Logic Programming · Hybrid Knowledge Base .

1 Introduction

Artificial Intelligence(AI) exhibits various applications in the aviation industry such as virtual assistants. Deploying a virtual assistant during flights enhances pilot proficiency and ensuring the seamless execution of flight operations. In this context, Thales plans to construct a virtual assistant using a symbolic AI system, which falls under the domain of AI. The entirety of information within the virtual assistant is systematically represented in its knowledge base using a KR language. Utilizing this knowledge base with other components, the virtual assistant guides pilots through the execution of varied tasks, facilitated by a sophisticated reasoner.

Some use cases of this virtual assistant include fault detection and troubleshooting, providing suggestions to pilots for improving flight performance,

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answering queries, and assisting in the decision-making process during critical situations. To execute these use cases, knowledge engineers represent contextual information along with instantaneous knowledge such as flight machinery data, meteorological data, and information from air traffic controllers in the knowledge base. This knowledge can be classified into three different types: static knowledge, which remains unchanged during flight; dynamic knowledge with infrequent updates and dynamic knowledge with periodic updates which changes during flights.

For the effective construction of a knowledge base, essential features include the Closed-World Assumption(CWA) means assuming false if something cannot be derived as true, beneficial for tasks like representing a list of airports, and the Open-World Assumption(OWA) means no conclusions is made from the absence of information, useful for use cases related to weather information. Also, we need to represent some procedural rules that help with fault detection and rectification. Additionally, Non-monotonic Reasoning, entails that new knowledge will invalidate the previously drawn conclusion, is required to perform reasoning over dynamic knowledge, which changes over time. A comprehensive solution to include all these features is to integrate two major KR concepts: Ontologies and Rules.

Ontologies are structured representations of knowledge within specific domains, that defines the type of entities that exist, properties that can be used to describe them, and relationships among those[28]. Description Logic(DL)s, a decidable variant of first-order logic is a widely accepted ontology language[1].

Rules capture knowledge about the world by expressing the IF-Then relationship, There are many varieties of rule languages. But in general, they can be divided into Production systems and Logic Programming(LP) systems[9]. Production systems express knowledge using conditional statements with a specific control flow and the Logic Programming system uses a declarative style which means modelling what should be achieved instead of how to achieve it.

LP and DLs have many distinct features. So combining both approaches will enhance the capabilities of a knowledge representation and reasoning system. In [27], define several benefits of LP over DLs. LP facilitates the representation of non-tree-like relationships, offering a more flexible and dynamic approach to expressing complex connections within a knowledge domain and operates under the CWA and is non-monotonic. N-ary predicates , ability to represent integrity constraints, and exception modeling are some of the other benefits of LP. Furthermore, the availability of highly optimized reasoners enhances the efficiency of reasoning processes.

Contrarily, DLs offers a rich set of constructors for complex entity connections and allow reasoning over abstract relationships without requiring concrete instances, known as Terminological Reasoning. Reasoning with DL is based on OWA and it is monotonic which means new knowledge doesn't invalidate the previously drawn conclusion. Various DLs can be defined based on the combination of different constructors offering flexibility to choose a language that matches the required expressivity. Moreover, DLs enable Open-domain Reason-

ing, accommodating an infinite number of anonymous individuals within their reasoning framework.

Overall, LPs are suited for data-centric reasoning tasks like query answering, while DLs stand out for their terminological reasoning capabilities and hierarchical representation style. Despite the benefits, there are several challenges we need to face while combining DLs and LP due to inherent differences in the semantics of both approaches [13],[31]. This includes managing default assumptions such as CWA and OWA, monotonicity, treatment of equality, domain, and negation choices(Weak Negation for LP and Explicit Negation for DLs). Furthermore, decidability is another concern during this reconciliation. However, several works are being published that address the aforementioned challenges and give solutions to solve them(explained in section 2.3).

2 State of the Art

This section is split into three parts, covering the languages and reasoners for LP systems and DLs separately, and also delving into works that combine both approaches.

2.1 Reasoning in Description Logics

The current standard for ontologies is the Web Ontology Language(OWL), rooted in DLs. OWL offers a range of variants offering diverse constructors, each with distinct computational complexities tailored for specific use cases. At one end, there's the most expressive variant, OWL Full[34], allowing for rich and complex modeling but undecidable, OWL 2 introduced more tractable variants, such as OWL 2 RL (Rule Language), OWL 2 EL (Existential Language), and OWL 2 QL (Query Language)[6]. Listing 1.1 defines a small Description Logic(DL) with a Terminological Box(TBox) that delineates the abstract relationship among classes and properties, and an Assertional Box(ABox) specifies instances of these classes and properties. Equivalent OWL syntax of this is mentioned in Listing 1.2.

Listing 1.1. Example DL ontology

```
<!-- Axioms/Terminological Box/TBox -->
TBox = {Parent subClass Human }.
<!-- Assertional Box/ABox/Instances -->
ABox = {Parent(individual_a)}.
#Reasoning Tasks
<!-- Subsumption Checking -->
?- subClass(Human,Parent). - Result: Yes.
<!-- Instance Checking -->
?- Human(individual_a). - Result:Yes.
<!-- Instance Retrieval -->
?- Human(X). - Result:individual_a.
```

Listing 1.2. Equivalent OWL Syntax

```
<!-- Axioms/Terminologies/TBox -->
<owl:Class rdf:about="#Human"/>
<owl:Class rdf:about="#Parent">
  <rdf:subClassOf rdf:resource="#Human"/>
</owl:Class>
<owl:Class rdf:about="#Father">
  <rdf:subClassOf rdf:resource="#Parent"/>
</owl:Class>
<!-- Assertions/ABox/Instances -->
<owl:NamedIndividual rdf:about="#individual_a">
  <rdf:type rdf:resource="#Human"/>
</owl:NamedIndividual>
```

In OWL languages, key reasoning tasks include consistency checking ensures logical coherence, instance checking verifying individual membership in specified concepts, subsumption checking for assessing concept hierarchy relationships and instance retrieval involves extracting relevant instances based on defined criteria. Several DL reasoning methodologies, such as Tableau-based algorithms, Classification, Rule-based DL reasoning, First-order Theorem prover-based DL reasoning, and DLE framework-based reasoning, are commonly employed to ex-

ecute the mentioned reasoning tasks. Tableau-based reasoning is a method that constructs proof trees to ascertain the consistency of DL ontologies employed by well-known reasoners such as Pellet[15] and HermiT[35]. ELK is a reasoner that utilizes classification, the process of determining the subsumption relationships between concepts within an ontology by applying inference rules[43]. Additional reasoning methods include rule-based DL reasoners by taking advantage of rule engines to perform efficient reasoning over very large ABox(RDFox), by using first-order theorem provers(Surnia[18], Hoolet[3] using Vampire Theorem Prover) and Description Logic Entailment(DLE) framework by combining the benefits of tableau algorithm for effective TBox reasoning and rule engines for ABox reasoning[26](DLE-Jena).

2.2 Reasoning in Logic Programming

Different LP systems include Answer Set Programming (ASP)[24], General Logic Programming[33], F-logic[21], and Constraint Logic Programming[38]. Notably, these declarative languages primarily focus on query answering as the principal reasoning task, except ASP, which encompasses tasks such as brave and cautious reasoning, and answer set checking. ASP focuses on generating answer sets, while other languages often utilize a backward chaining approach, attempting to prove the query by tracing back from known evidence. For General Logic Programming, reasoning engines such as SWI-Prolog, XSB Prolog, and B-prolog are commonly employed. In ASP, dedicated reasoning engines such as Clingo, DLV, S-Models and F-logic rely on engines like Florid and Flora2.

2.3 Combining DLs and LP System

Numerous research endeavours have explored the amalgamation of DLs and LP, leading to a categorization of below integration methods based on the intended semantics of the combined language, its expressivity, and the nature of the interaction between them. Broadly, the integration strategies can be distilled into two overarching approaches based on the semantics of the integrated languages: the Homogeneous Approach and the Hybrid Approach[14],[11].

Homogeneous Integration utilized a unified language with a single semantics that embedded both DLs and rules. Based on the expressivity, we can further classify Homogeneous integration into monotonic and quasi-monotonic approaches (also called Full Integration or Embedding Approach).

Monotonic approach is mainly focused on first-order semantics and employs only open-world assumption. Semantic Web Rule Language(SWRL)[20], a union of DLs and Horn Logic is considered as a language of this approach. But in general, SWRL is considered undecidable, so various tractable forms were invented which include Description Logic Program(DLP)[4], Description Logic Rules[22], DL Safe Rules[22], and Existential Logic Program(ELP)[22]. There are mainly three ways to construct a reasoner for this approach: using a first-order theorem prover, an OWL reasoner, or a rule engine. In all these cases, we need to use a translator to convert either rules or DLs or both to the language accepted by the reasoner.

Quasi-monotonic approach extends the above approach by adding non-monotonic features by utilizing the extensions of first-order logics such as circumscription, default logic, and defeasible logic. In this approach, both open-world and closed-world assumptions are employed to execute the reasoning tasks. MKNF+[7] and Hybrid MKNF[25], based on auto-epistemic logic and DR-logic[5] based on defeasible logic are some of the existing languages for this approach. Also, open-answer set[36] and first-order stable model semantics[29] can serve as unifying logic system to embedded both LP and DLs. Some works includes Extended Forest Logic Program and Guarded Hybrid Knowledge base[19] can illustrate this. We can construct a reasoner for this approach by using meta programming with a rule engine to guarantee the semantics of the language. NoHr Reasoner is a query answering tool based on Hybrid MKNF, which uses XSB Prolog as the backend and uses a direct translator for OWL to LP conversion[41]. NoHr supports the tractable forms of OWL such as OWL 2 RL, OWL 2 EL, and OWL 2 QL. Also, there exists a prototype implementation of DR-Prolog, which uses the same XSB Prolog as backend.

In **Hybrid Integration**, two distinct semantics coexist, one dedicated to DLs and the other tailored to LP. Based on how DL and LP interact, we can further classify the hybrid integration into two types, Loose and Tight Integration[12].

In **Loose Integration**, the DL and LP components are treated as distinct entities that share knowledge by exchanging the logical consequences derived from each other. DL-Program employs loose integration that use DL queries in the body of the rules that interact with the DL component[40]. Several implementations such as NLP-DL[39], a web interface using Racer and DLV, DReW System[17] utilizing DLV and DL to LP translator and F-Logic#[37] appointing onto-broker engines(both f-logic and DL), are built on DL-programs. DLV-Hex, built upon the Hex system, can also be regarded as a reasoner for DL-Programs."

In **Tight Integration**, the interaction between LP and the DL part occurs at the level of the semantics of both components. In this approach, a shared model for both LP and DL is established and computed by deriving a model for DL under first-order semantics. Subsequently, the model of LP is computed by employing either well-founded semantics or stable-model semantics after eliminating the DL atoms by utilizing the initially derived DL model. So for each DL model, there exists a corresponding LP model. DL-Log under stable model semantics[30] and HD-Rules under well-founded semantics[42] are some of the existing languages that use tight integration. Also, there exists a prototype reasoner for HD-Rules as a web interface that uses Pellet and XSB Prolog as the backend. Additionally, there is an extension for DL-Log called Clopen knowledge, which introduces the capability to employ CWA within DLs[23].

In addition to this, within Hybrid Integration, there is a third approach that blends the characteristics of loose and tight coupling which can be called **Flexible Integration**. Resilient Logic Program is an example of this kind of approach[32].

3 Problem Statement

The prerequisites for the deployment of a Semantic Web system are explained in [8]. Essential components include declarative rules, enabling the generation of new data from pre-existing datasets, integrity constraints to ensure data consistency, ontologies for defining concepts and their interrelations, and procedural rules, which specify how the data can be modified depending on the current state. Furthermore, we need monotonic and non-monotonic negation.

The Monotonic approach, while a straightforward methodology, lacks certain features such as non-monotonic negation and integrity constraints. DL-program and DL+Log cannot express integrity constraints[10], reactive rules and cannot express CWA inside DLs. While DLV-Hex, a reasoner for Hex language, offers the capability to express reactive rules through external plugins(for example, using a Python plugin). However, its efficiency diminishes with larger knowledge bases due to inherent architectural constraints. Moreover, quasi-monotonic approaches like MKNF, though promising, present challenges. But the semantics of such approaches are difficult for knowledge engineers to grasp. Also, we need syntactic restrictions and limit the expressivity to build a practical reasoner due to decidability issues. So the pursuit of a practical reasoner with the aforementioned functionalities remains ongoing, signifying a critical area for advancement in semantic web systems.

Our objective is to develop a practical reasoner that not only incorporates the aforementioned features but also addresses additional requirements needed for the virtual assistant. To guide our research efforts effectively, we have formulated the following research question, delineating the specific areas under investigation:

RQ1 - How to combine DLs with LP system? This research question will be addressed by exploring four sub-research questions defined below:

RQ1.1 - What functional and non-functional requirements does the application domain expect from the integrated KR system?

Functional requirements address expressivity, information flow, the default assumptions for a rule, and DL predicates, emphasizing theoretical aspects. Non-functional requirements define characteristics such as query-answering performance, scalability, efficiency, and real-time reasoning performance, predominantly at the reasoner implementation level.

RQ1.2 - Which kind of knowledge is better suited for modelling with DL, conversely, which one is more effectively represented through LP? Carefully evaluating specific criteria is crucial when deciding whether to employ rules, Description Logic (DL), or both to model a particular use case.

RQ1.3 - What are the existing methods to integrate DLs with LP? For each method, answer the two sub-research questions defined below:

RQ1.3.1 - Any implementations are available?

RQ1.3.2 - Will this approach satisfy all the needed requirements?

- RQ2 - How to define the semantics of a language that integrates LP and DL to fulfil the functional requirements of this application domain?** The answer to this research question depends upon RQ1 (specifically, SRQ3) to identify or invent suitable semantics to combine LP and DL. This research question also aims to study the decidability and tractability of the language and discusses the constraints to enable it.
- RQ3 - How to perform essential reasoning tasks such as query answering?** This question aims to build a reasoner that adheres to the defined declarative semantics of the language.
- RQ3.1 - What architecture and algorithms are most appropriate for this?** Two approaches exist for constructing a reasoner for the integrated language: a single rule reasoner or a coupled two-reasoner setup. And when it comes to algorithms, options include forward chaining and backward chaining systems. So identifying an effective methodology to construct the reasoner is pivotal.
- RQ3.2 - Is it possible to utilize existing tools for implementation, and if so, which one is the most suitable?** Identifying the most efficient tool for implementing the operational semantics to execute the required reasoning task.
- RQ3.3 - How to optimize the execution of reasoning tasks to achieve optimal results?** Optimization techniques at both the algorithmic and implementation levels are explored to meet the non-functional requirements of the application domain.

4 Research Methodology

This research is structured into three distinct phases to address the aforementioned research questions: the State of the Art Phase, Experimentation Phase, and Evaluation phase. The objective of the state-of-the-art phase is to explore existing methods that combine LP and DLs. This includes grasping the theory behind each approach and testing them at both theoretical and practical levels to uncover any limitations with respect to the functional requirements of the virtual assistant. Subsequently, we aim to pinpoint necessary improvements to enhance these approaches to meet the requirements of a virtual assistant. During the experimentation phase, we leverage insights from the previous stage to devise a methodology that addresses the identified limitations. This involves constructing an optimized reasoner obeying non-functional requirements. Finally, in the evaluation phase, we conduct a thorough comparison between our methodology and existing approaches to validate whether our objectives have been met. This rigorous evaluation ensures that our proposed methodology satisfies the needs of the virtual assistant effectively.

5 Evaluation Plan

We need to evaluate the result of this thesis theoretically by implementing the use cases to ascertain the fulfilment of the functional requirements. Key parameters

for assessment include **Expressivity**(as described in section 3), **Information Flow, Domain, and Negation choices for DL and LP Predicates**. As requirements evolve, additional parameters will be integrated.

Besides this, we need a quantitative evaluation to analyze the non-functional requirements. We decided to use existing OWL benchmarks incorporating a rule base with it. To do the initial testing, we utilize OWL2Bench, a dataset capable of generating a DL knowledge base and an extension of University Ontology Benchmark (UOBM) with a TBox encompasses four OWL languages(OWL 2 RL, OWL 2 QL, OWL 2 EL, OWL 2 DL) with all possible constructors and an ABox generator of variable size[16]. Selected parameters to evaluate non-functional requirements include **Query Answering Performance, Scalability, Query Result Comparison** using the Jaccard Similarity index[2], **Real-time Reasoning Performance and Timeliness**, and **Efficiency**. If existing benchmarks prove inadequate, there is a plan to develop an in-house benchmark that integrates both DL and LP to perform the evaluation.

6 Preliminary Result

Answering RQ1.1, the functional requirement involves defining a Knowledge Representation language capable of expressing various virtual assistant use cases, where certain scenarios require evaluation under an open-world assumption and others under a closed-world assumption. Additionally, there is a need for bidirectional information exchange between these cases. Also, the KR system must be able to capture and reason with the real-time data generated in flight. However, additional requirements including expressivity and specific reasoning tasks required for operational use-cases of the virtual assistant are yet to be defined. Also, the reasoner must be capable of providing explanations regarding how inferences are derived. Addressing non-functional requirements, the KR system must exhibit good reasoning performance, scalability, real-time reasoning capabilities, and efficiency in terms of resource consumption. **RQ1.3** is addressed in section

Homogeneous - Monotonic	Homogeneous - Quasi-Monotonic	Hybrid - Loose Integration	Hybrid - Tight Integration
First-order(FO) Semantics	FO Non-Monotonic Semantics	DL under FO Semantics, Rules under NM semantics	DL under FO Semantics, Rules under NM semantics
Intralingual	Intralingual	Logical Consequences	Model-Based
Only OWA	OWA and CWA for Rules and DL atoms	OWA for DL atoms, CWA for Rule atoms	OWA for DL atoms, CWA for Rule atoms
Both rule and DL atoms are open	Open and closed atoms are allowed in both rules and DL	DL atoms are open, Rule atoms are closed	DL atoms are open, Rule atoms are closed
SWRL	Hybrid MKNF	DL-Program	DL-Log, HD-Rules

Table 1. Different ways to integrate Rules and DL

2.3 and Table 1 illustrates the general features of methods to combine LP and DLs (Row 1) , including semantics (Row 2) , the interaction between LP and DL

components (Row 3), default assumptions (Row 4), the domain consideration (Row 5), and a review of existing works (Row 6).

We planned to start working with a Loose integration approach, which is a very simple way to integrate LP and DLs. DL-program which is a promising work based on loose integration and also, there are some prototype reasoners available. Test them to understand their limitations, and subsequently decide on improvements or explore alternative integration types.

7 Conclusion and Future Work

In the above sections, we outlined our research plan to execute this thesis and provided an overview of our initial results. As a first step, we identified the initial requirements needed for this application domain and identified existing methods to combine LP and DLs. From the list, we choose one method for studying and Our chosen framework is the program.

Our next step is to perform evaluations on DL-program concerning identified functional and non-functional requirements. Then recognize the improvement needed for the approach to apply in this context or consider pursuing an alternative approach. Also, illustrate a protocol for knowledge engineers to select either LP or DL while modelling a use case.

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